

# Electrochemistry for materials technology

Chapter 4B

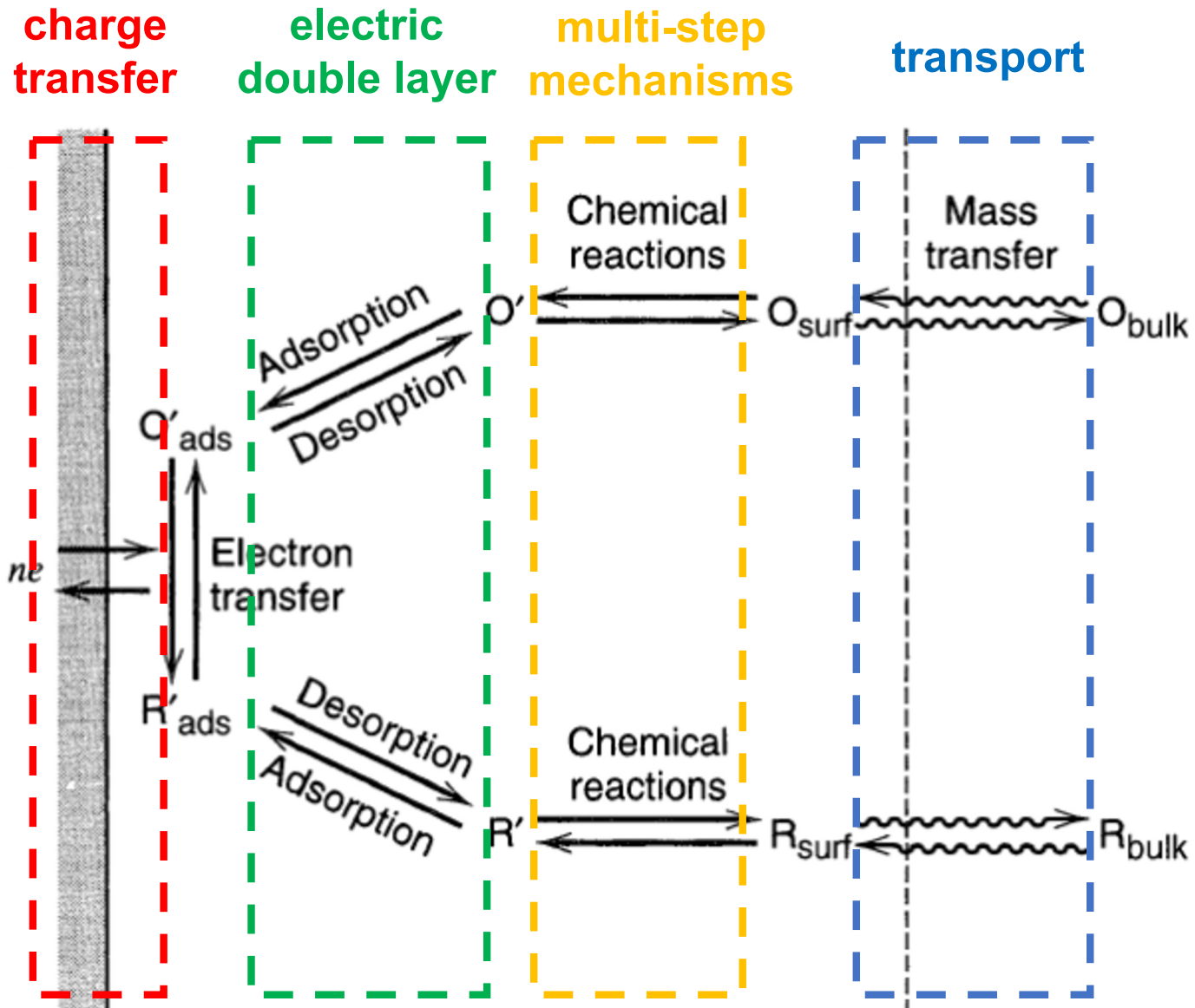
Electrode kinetics

**Mass transport phenomena**

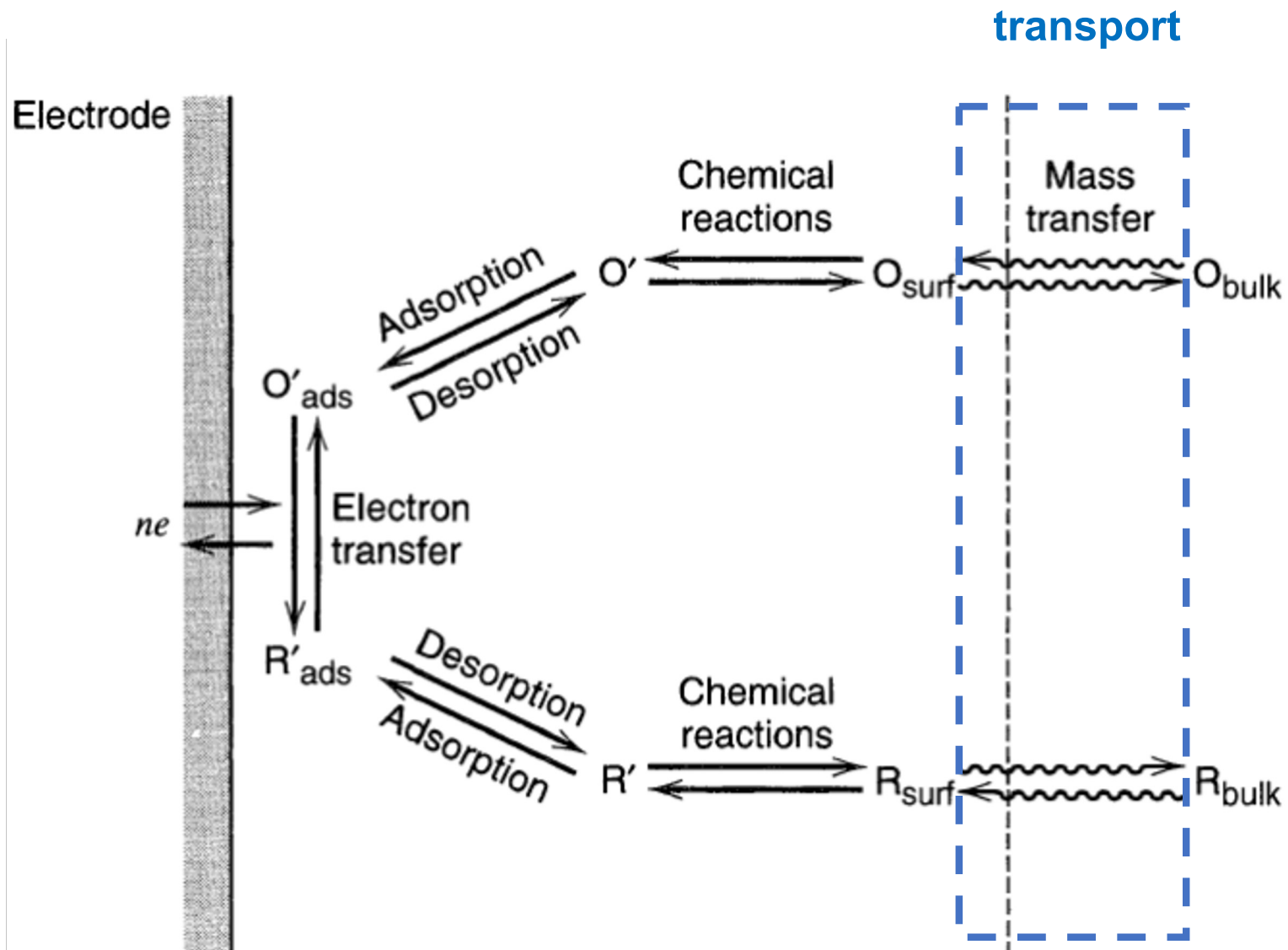
# Transport Phenomena

- Diffusion
- Diffusion + Migration
- Convection
- Transient Responses

# B-V Model with Mass Transport



# B-V Model with Mass Transport



# Modes of Mass Transport

**Diffusion** : movement of a species under the influence of a gradient of chemical potential (i.e., a **concentration gradient**).

**Migration** : movement of a charged species under the influence of an electric field (a **gradient of electrical potential**).

**Convection** : stirring or hydrodynamic transport (may be characterized by stagnant regions, laminar flow, or turbulent flow).

# Modes of Mass Transport

Mass transfer to an electrode is governed by the **Nernst-Planck equation** written for one-dimensional mass transfer along the x-axis as:

$$J_i(x) = \underbrace{-D_i \frac{\partial C_i(x)}{\partial x}}_{\text{diffusion}} - \underbrace{\frac{z_i F}{RT} D_i C_i \frac{\partial \Phi(x)}{\partial x}}_{\text{migration}} + \underbrace{C_i v(x)}_{\text{convection}}$$

*mol/m<sup>3</sup>*

$J_i(x)$  : flux of species i at a distance x from the surface [ $\text{mol s}^{-1} \text{ cm}^{-2}$ ]

$D_i(x)$  : diffusion coefficient of species i [ $\text{cm}^2/\text{s}$ ]

$\frac{\partial C_i(x)}{\partial x}$  : concentration gradient at distance x

$\frac{\partial \Phi(x)}{\partial x}$  : potential gradient at distance x  $\text{Volt} / \text{m}$

$z_i$  : charge of species i (not to be confused with z, which is mol e<sup>-</sup> /mol reactant)


$C_i$  : concentration of species i [ $\text{mol cm}^{-3}$ ]

$v(x)$ : velocity with which a volume element in solution moves along the axis [ $\text{cm s}^{-1}$ ]

# Modes of Mass Transport

A rigorous solution is not easy when all 3 forms of mass transfer are present; hence electrochemical systems are frequently designed so that one or more of the contributions to mass transfer are negligible.

For example,

**Migration** can be considered negligible by the addition of inert electrolyte (i.e. a supporting electrolyte) at a concentration much larger than that of the electroactive species.  screens the electric field that is “felt” by the reactive species

**Convection** can be considered negligible by preventing stirring and vibrations in the (‘stagnant’) electrochemical cell.

# Mass Transport without convection

Mass transfer to an electrode is governed by the **Nernst-Planck equation** written for one-dimensional mass transfer along the x-axis as:

$$J_i(x) = \underbrace{-D_i \frac{\partial C_i(x)}{\partial x}}_{\text{diffusion}} - \underbrace{\frac{z_i F}{RT} D_i C_i \frac{\partial \Phi(x)}{\partial x}}_{\text{migration}} + \cancel{C_i v(x)}$$

If the species  $i$  is charged, then the flux,  $J_i$ , is equivalent to a current density  $j_i$ :

$$-J_i = \frac{j_i}{z_i F} = \underbrace{\frac{j_{d,i}}{z_i F}}_{\text{flux due to diffusion}} + \underbrace{\frac{j_{m,i}}{z_i F}}_{\text{flux due to migration}}$$

charge of species  $i$  (pointing to  $z_i F$ )

$$\frac{j_{d,i}}{z_i F} = D_i \frac{\partial C_i(x)}{\partial x}$$

$$\frac{j_{m,i}}{z_i F} = \frac{z_i F}{RT} D_i C_i \frac{\partial \Phi(x)}{\partial x}$$

# Mass Transport without convection

At any location in solution, the total current is made up of contributions from all the species  $i$  :

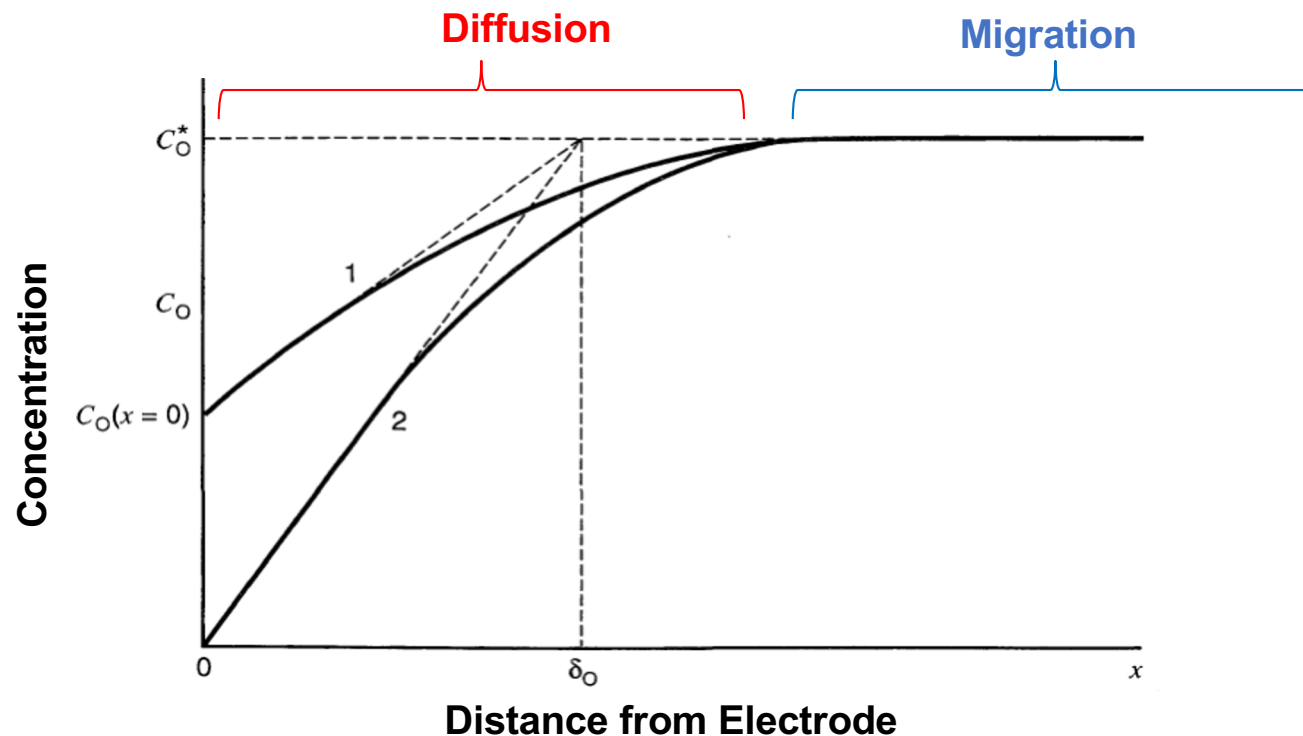
$$j = \sum_i j_i = \sum_i (j_{d,i} + j_{m,i}) = F \sum_i z_i D_i \frac{\partial C_i(x)}{\partial x} + \frac{F^2}{RT} \frac{\partial \Phi(x)}{\partial x} \sum_i z_i^2 D_i C_i$$

where the current for each species at that location is made up of a **diffusional component** and a **migrational component**

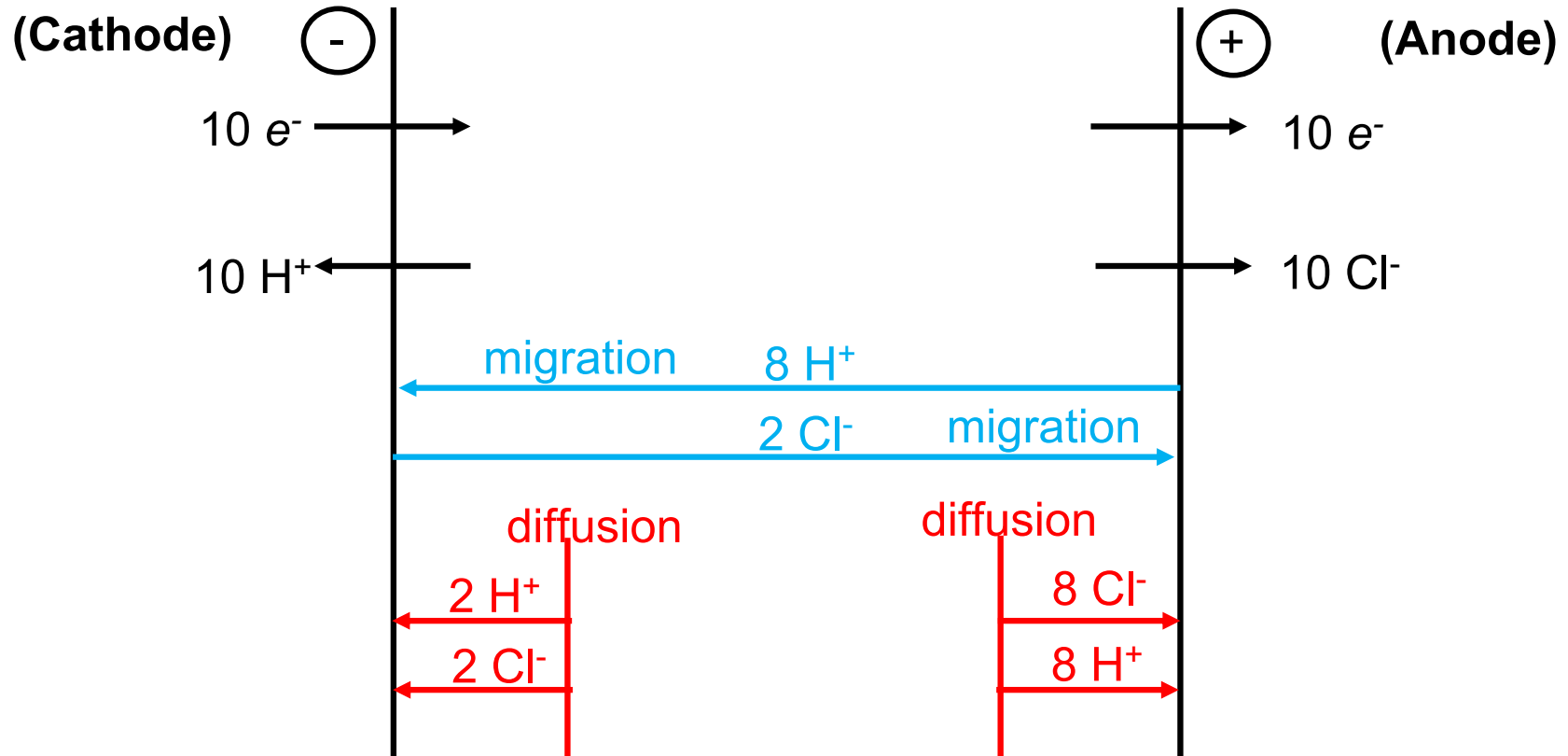
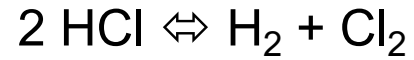
# Mass Transport without convection

The relative contributions of diffusion and migration to the flux of a species (and the flux of that species to the total current) differ for different locations in solution.

- Far from the electrode, migration can play a dominant role.
- Near an electrode, an electroactive substance is usually transported by both processes.



# Mass Transport without convection



**Cathode:**  
80% of  $\text{H}^+$  current is migration

**Anode:**  
20% of  $\text{Cl}^-$  current is migration

# Migration

In the bulk solution (away from the electrode), concentration gradients are generally small, and the total current is carried mainly by migration of all charged species.

$$j_i = \cancel{j_{d,i}} + j_{m,i} = F z_i D_i \cancel{\frac{\partial C_i(x)}{\partial x}} + \frac{F^2}{RT} \frac{\partial \Phi(x)}{\partial x} z_i^2 D_i C_i$$

small concentration  
gradient

$$j_i = \frac{z_i^2 F^2 D_i C_i}{RT} \frac{\partial \Phi(x)}{\partial x}$$

# Migration

$$j_{m,i} = \frac{z_i^2 F^2}{RT} D_i C_i \frac{\partial \Phi(x)}{\partial x}$$

**Mobility** of a species **i** ( $u_i$ ) is the ability of a charged particle to move through a medium in response to an electric field.

$$u_i = \frac{|z_i| F D_i}{RT} \quad \text{unit: m}^2/\text{V.s}$$

By substituting for  $D_i$ ,

assuming linear change in  
potential ( $\Delta E$ ) over distance  $L$

$$j_{m,i} = |z_i| F u_i C_i \frac{\partial \Phi(x)}{\partial x} \quad \longrightarrow \quad j_{m,i} = \frac{|z_i| F u_i C_i \Delta E}{L}$$

$\frac{\partial \Phi(x)}{\partial x} \sim \frac{\Delta E}{L}$

# Migration

If multiple species  $i$  contribute to current, the total current is the sum of all the individual contributions.

$$j = \sum_i j_i = \frac{F\Delta E}{L} \sum_i |z_i| u_i C_i$$

The **transference number  $t_i$**  of species  $i$  is the fraction of the total migration current that a given ion  $i$  carries.

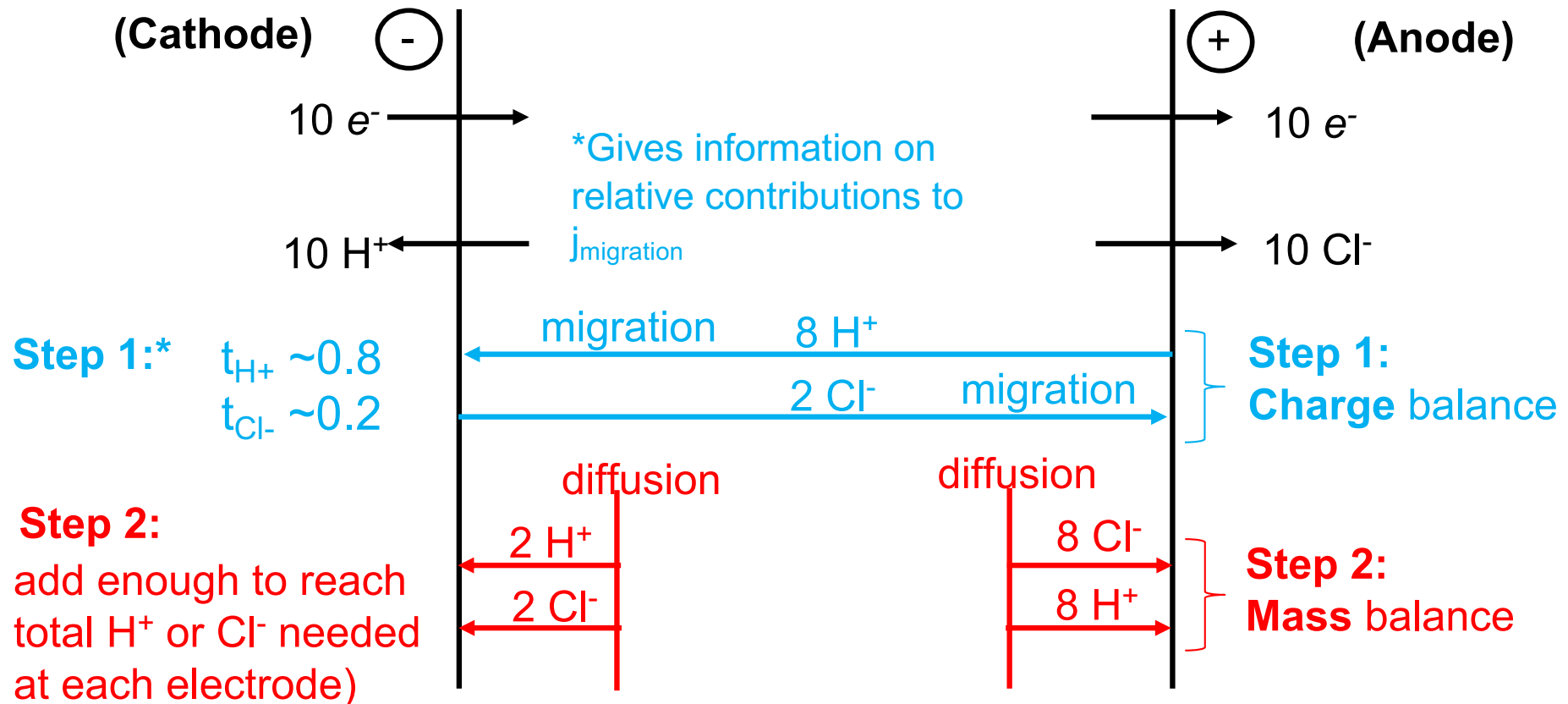
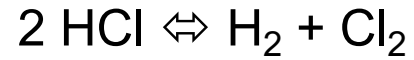
$$t_i = \frac{j_i}{j} = \frac{|z_i| u_i C_i}{\sum_k |z_k| u_k C_k}$$

$C_i$  = concentration of  $i$

$z_i$  = charge of  $i$

$u_i$  = mobility of  $i$

# Mixed Migration + Diffusion



**Cathode:**

**80% of  $\text{H}^+$  current is migration\*\***

\*\*gives information on  $j_{\text{migration}}$  VS.  $j_{\text{diffusion}}$

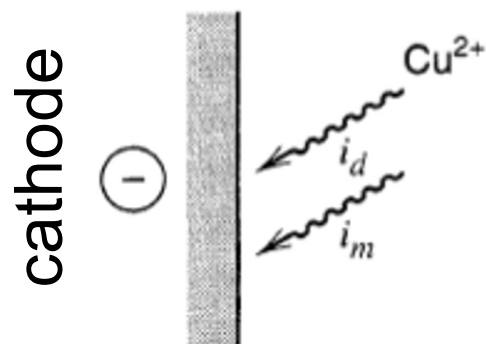
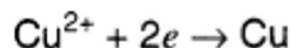
independent of  $t_{\text{H}^+}$ ,  $t_{\text{Cl}^-}$  (happens to also be 0.8, 0.2 in this example)

**Anode:**

**20% of  $\text{Cl}^-$  current is migration\*\***

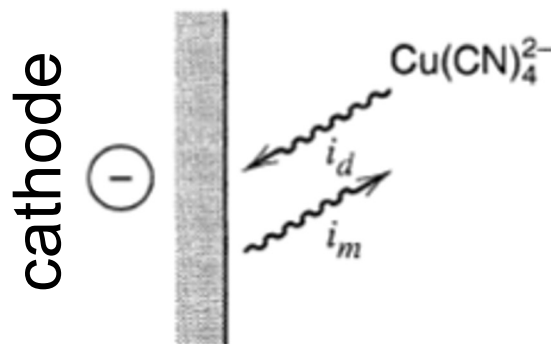
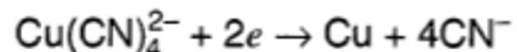
# Mixed Migration + Diffusion

## Positively charged reactant



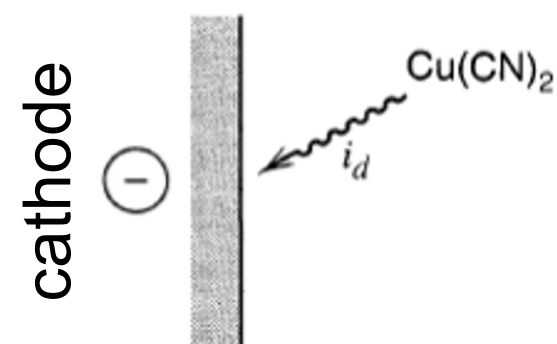
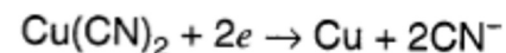
$$j = j_d + |j_m|$$

## Negatively charged reactant



$$j = j_d - |j_m|$$

## Uncharged reactant



$$j = j_d$$

Migrational component is **same direction** as  $j_d$  for

- Cations reacting at cathode
- Anions reacting at anode

Migrational component is **different direction** from  $j_d$  for

- Cations oxidized at anodes
- Anions reduced at cathodes

# Sign Convention for Diffusion and Migration Currents (see previous slide)

## Diffusion current ( $j_d$ )

- ⊕ Oxidized species diffuses to cathode (increases cathodic current by making it more negative)
- ⊕ Reduced species diffuses to anode (increases anodic current by making it more positive)

## Migration current ( $j_m$ )

- ⊕ Cation migrates to cathode (increases cathodic current by making it more negative)
- ⊕ Anion migrates to anode (increases migration anodic current by making it more positive)
- ⊖ Anion diffuses to cathode (decreases cathodic current by making it less negative)
- ⊖ Cation diffuses to anode (decreases anodic current by making it less positive)

# Diffusion-limited case

Consider the reduction reaction



when the reduction of O begins,  $[O]_s \ll [O]^*$

$$J_i(x) = \underbrace{-D_i \frac{\partial C_i(x)}{\partial x}}_{\text{diffusion}} - \cancel{\frac{z_i F}{RT} D_i C_i \frac{\partial \Phi(x)}{\partial x}} + \cancel{C_i v(x)}$$

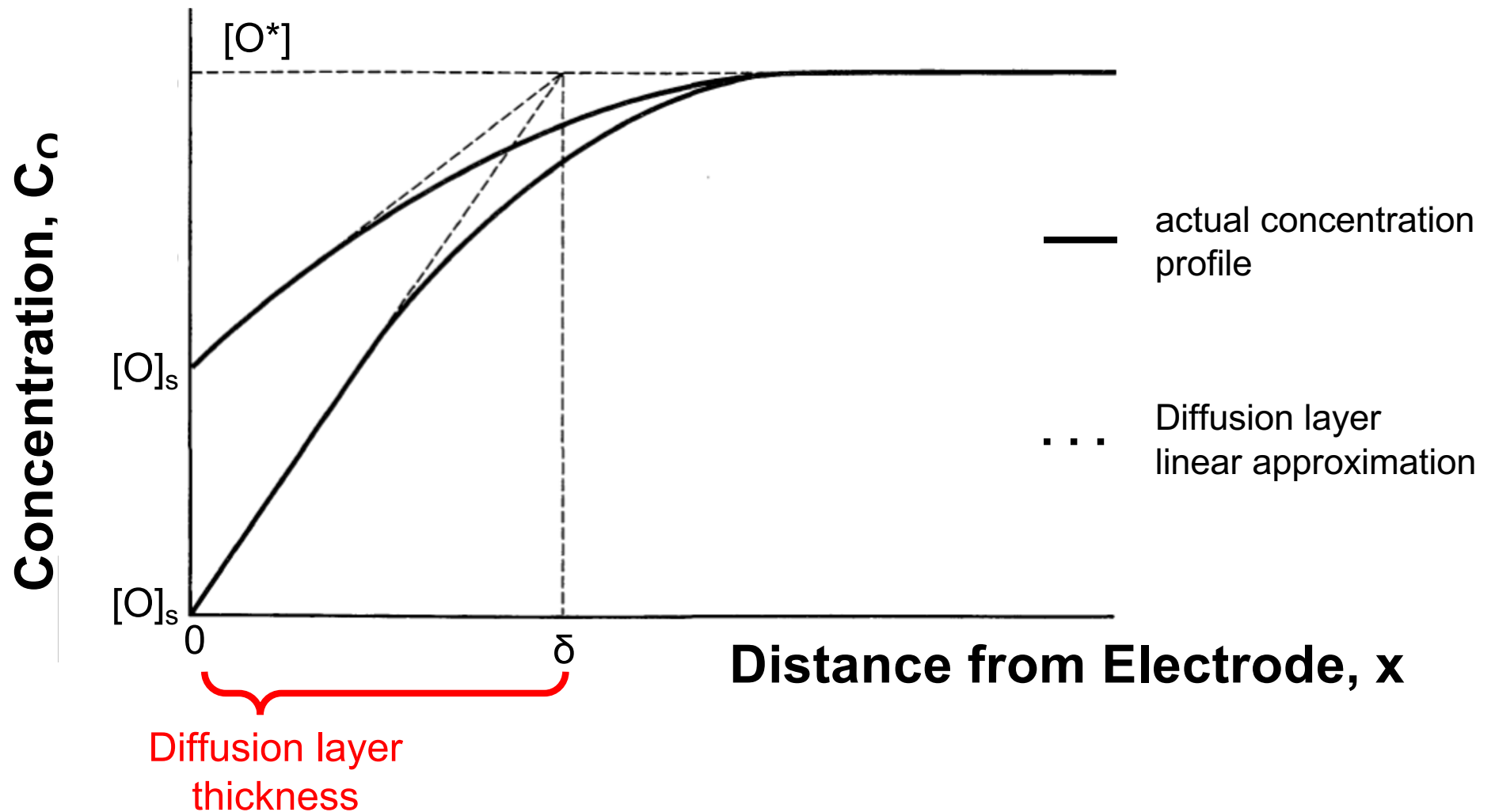
assume there is an excess of supporting electrolyte
assume stirring is ineffective at the electrode surface

Rate of mass-transfer ( $v_{mt}$ ) is proportional to the concentration gradient

$$v_{mt} \propto D_O \left. \frac{\partial C_O(x)}{\partial x} \right|_{x=0} \xrightarrow{\text{assuming linear variation}} D_O \frac{[O]^* - [O]_s}{\delta}$$

(at the surface)

# Diffusion-limited case



# Linear diffusion approximation:

## 1) R initially absent

Consider the reaction



Recall in our derivation of the mass-transfer limited Butler-Volmer expression:

**O is consumed,  $[\text{O}]_s < [\text{O}^*]$ :**

$$j = k_{m,\text{O}}([\text{O}]_s - [\text{O}^*]) \cdot z \cdot F$$

**R is produced,  $[\text{R}]_s > [\text{R}^*]$ :**

$$j = k_{m,\text{R}}([\text{R}^*] - [\text{R}]_s) \cdot z \cdot F$$

For limiting case where  $[\text{O}]_s = 0$ ,

$$j_{\text{lim},c} = -k_{m,\text{O}}[\text{O}^*] \cdot z \cdot F$$

$$[\text{O}]_s = \frac{j - j_{\text{lim},c}}{k_{m,\text{O}} \cdot z \cdot F}$$

For limiting case where  $[\text{R}^*] = 0$ ,

$$j = -k_{m,\text{R}}[\text{R}]_s \cdot z \cdot F$$

$$[\text{R}]_s = \frac{-j}{k_{m,\text{R}} \cdot z \cdot F}$$

# Linear diffusion approximation:

## 1) R initially absent

If the kinetics are fast, the concentrations of O and R at the electrode surface can be assumed to be at equilibrium:

### Nernst Equation

$$E_{\text{cell}} = E^{\circ}_{\text{cell},T} - \frac{RT}{zF} \ln \frac{[R]_s}{[O]_s} \quad \text{substitution} = E^{\circ}_{\text{cell},T} - \frac{RT}{zF} \ln \frac{-j}{k_{m,R} \cdot z \cdot F} \cdot \frac{k_{m,O} \cdot z \cdot F}{j - j_{\text{lim},c}}$$

$$E_{\text{cell}} = E^{\circ}_{\text{cell},T} - \frac{RT}{zF} \ln \frac{k_{m,O}}{k_{m,R}} + \frac{RT}{zF} \ln \frac{j - j_{\text{lim},c}}{-j}$$

when  $j = j_{\text{lim},c}/2$

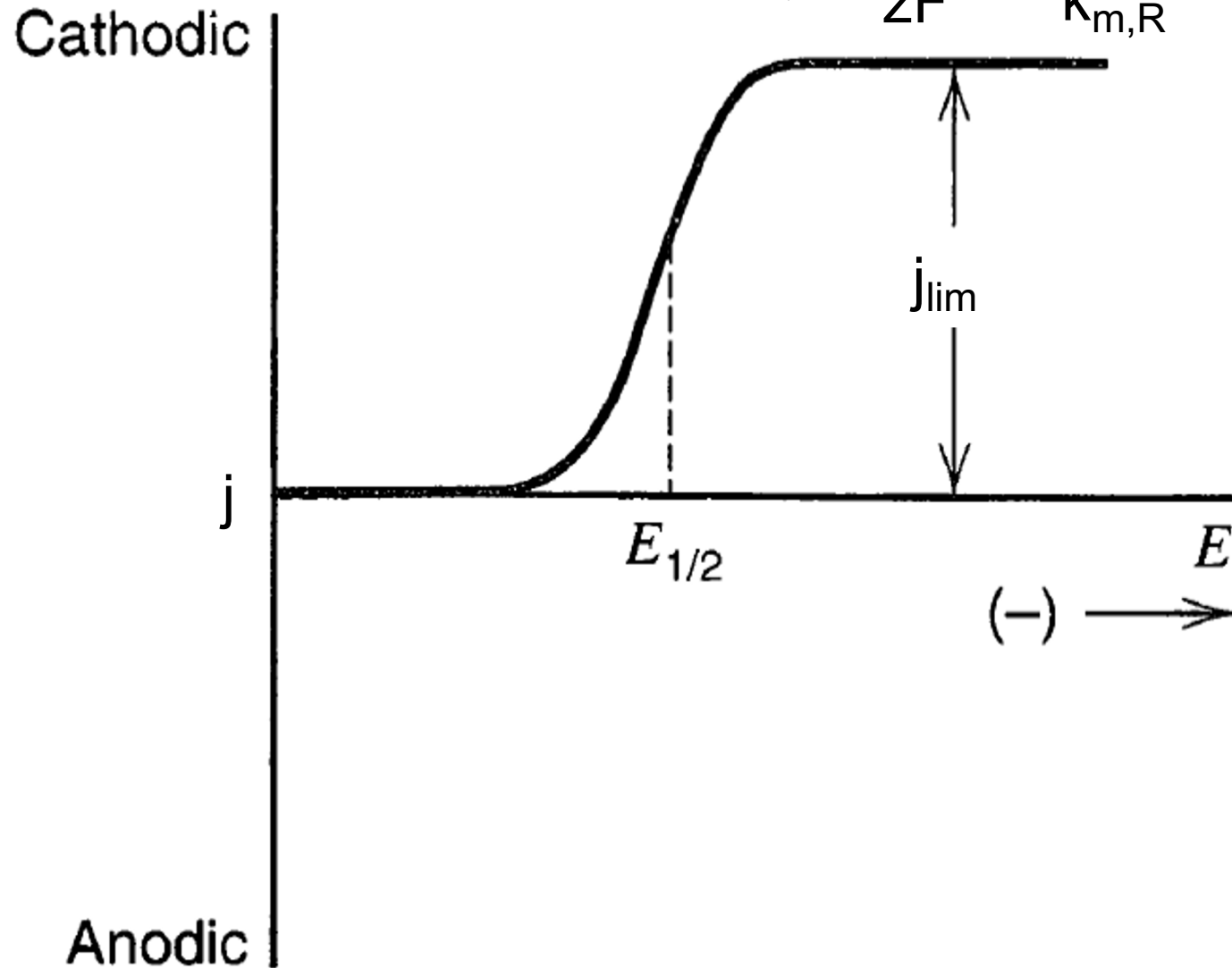
0

$$E_{1/2} = E^{\circ}_{\text{cell},T} - \frac{RT}{zF} \ln \frac{k_{m,O}}{k_{m,R}}$$

when  $k_{m,O} \sim k_{m,R}$ ,  
 $E_{1/2} \sim E^{\circ}_{\text{cell},T}$

# Linear diffusion approximation: 1) R initially absent

$$E_{1/2} = E^{\circ}_{\text{cell},T} - \frac{RT}{zF} \ln \frac{k_{m,O}}{k_{m,R}}$$



# Linear diffusion approximation:

## 1) R initially absent

If the kinetics are fast, the concentrations of O and R at the electrode surface can be assumed to be at equilibrium:

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$$E_{\text{cell}} = E^{\circ}_{\text{cell},T} - \frac{RT}{zF} \ln \frac{k_{m,O}}{k_{m,R}} + \frac{RT}{zF} \ln \frac{j - j_{\text{lim},c}}{-j}$$

when  $j = j_{\text{lim},c}/2$   $E_{1/2}$  is a characteristic of the system

$$E_{1/2} = E^{\circ}_{\text{cell},T} - \frac{RT}{zF} \ln \frac{k_{m,O}}{k_{m,R}}$$

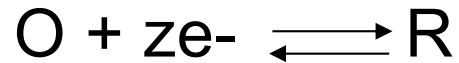


$$E_{\text{cell}} = E_{1/2} + \frac{RT}{zF} \ln \frac{j - j_{\text{lim},c}}{-j}$$

# Linear diffusion approximation:

## 2) O and R initially present

Consider the reaction



Recall in our derivation of the mass-transfer limited Butler-Volmer expression:

**O concentration gradient:**

$$j = k_{m,O}([O]_s - [O^*]) \cdot z \cdot F$$

For limiting case where  $[O]_s=0$ ,

$$j_{lim,c} = -k_{m,O}[O^*] \cdot z \cdot F$$

$$[O]_s = \frac{j - j_{lim,c}}{k_{m,O} \cdot z \cdot F}$$

**R concentration gradient:**

$$j = k_{m,R}([R^*] - [R]_s) \cdot z \cdot F$$

For limiting case where  $[R]_s=0$ ,

$$j_{lim,a} = k_{m,R}[R^*] \cdot z \cdot F$$

$$[R]_s = \frac{j_{lim,a} - j}{k_{m,R} \cdot z \cdot F}$$

# Linear diffusion approximation:

## 2) O and R initially present

If the kinetics are fast, the concentrations of O and R at the electrode surface can be assumed to be at equilibrium:

### Nernst Equation

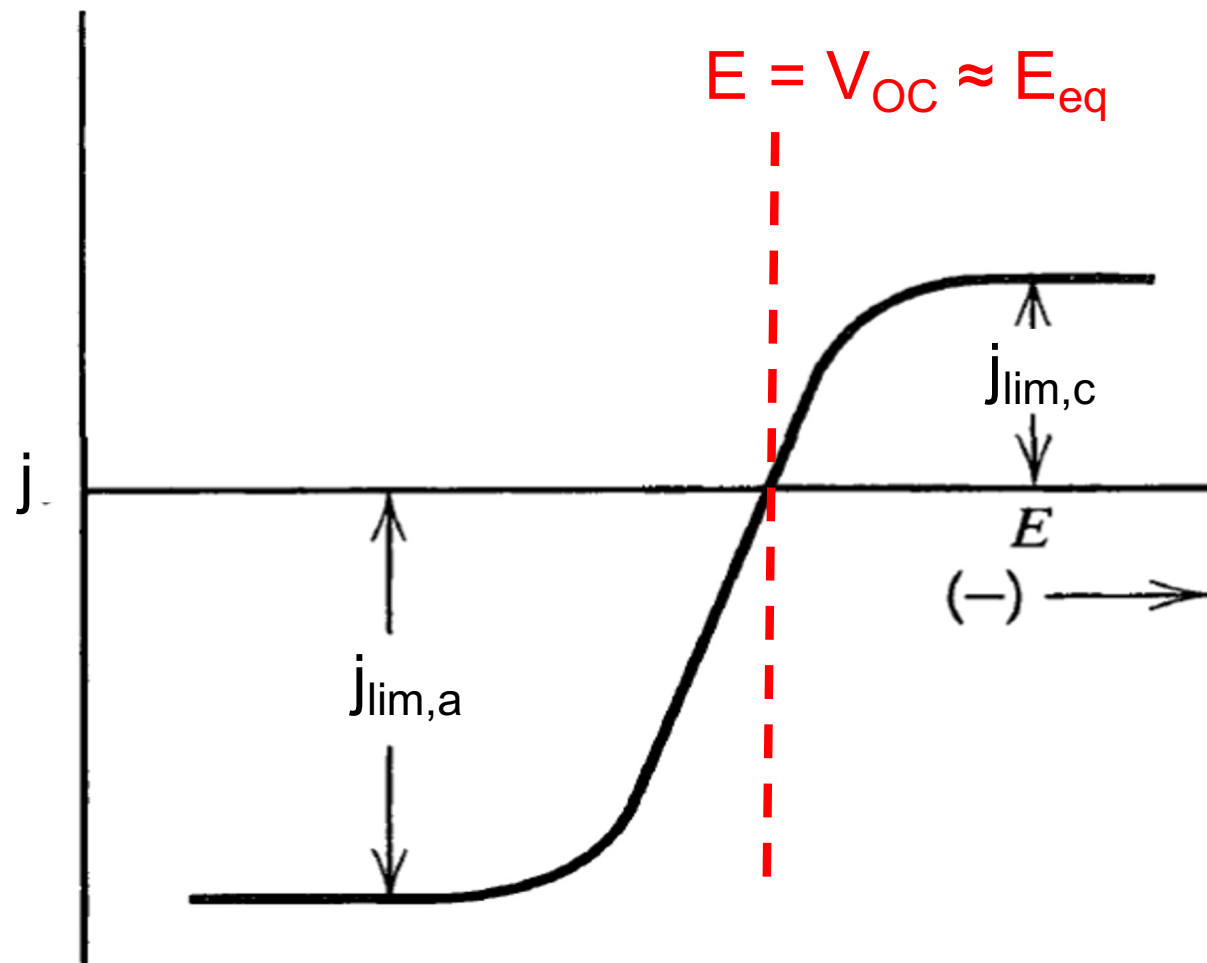
$$E_{\text{cell}} = E^{\circ}_{\text{cell},T} - \frac{RT}{zF} \ln \frac{[R]_s}{[O]_s} \quad \text{substitution} = E^{\circ}_{\text{cell},T} - \frac{RT}{zF} \ln \frac{j_{\text{lim},a} - j}{k_{m,R} \cdot z \cdot F} \cdot \frac{k_{m,O} \cdot z \cdot F}{j - j_{\text{lim},c}}$$

$$E_{\text{cell}} = E^{\circ}_{\text{cell},T} - \frac{RT}{zF} \ln \frac{k_{m,O}}{k_{m,R}} + \frac{RT}{zF} \ln \frac{j - j_{\text{lim},c}}{j_{\text{lim},a} - j}$$

# Linear diffusion approximation:

## 2) O and R initially present

When  $j = 0$ ,  $E = E_{eq}$  and the system is at equilibrium. When current flows, the potential deviates from  $E_{eq}$ , and the extent of this deviation is the concentration overpotential.



# Linear diffusion approximation:

## 3) R is insoluble

Suppose R is a metal and can thus be considered to be at essentially unit activity ( $a_R=1$ ) as the electrode reaction takes place on bulk R.

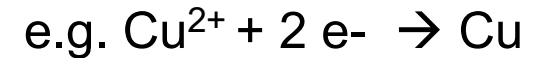
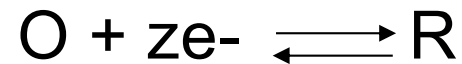
### Nernst Equation

$$E_{\text{cell}} = E^{\circ}_{\text{cell},T} + \frac{RT}{zF} \ln [\text{O}]_s$$

# Linear diffusion approximation:

## 3) R is insoluble

Consider the reaction



Recall in our derivation of the mass-transfer limited Butler-Volmer expression:

**O is consumed,  $[O]_s < [O^*]$ :**

$$j = k_{m,O}([O]_s - [O^*]) \cdot z \cdot F$$

(cf. Chapter 4A, slide 17)

For limiting case where  $[O]_s = 0$ ,

$$j_{\text{lim},c} = -k_{m,O}[O^*] \cdot z \cdot F$$

$$\frac{[O]_s}{[O^*]} = 1 - \frac{j}{j_{\text{lim},c}}$$

$$[O]_s = \frac{j - j_{\text{lim},c}}{k_{m,O} \cdot z \cdot F}$$

# Linear diffusion approximation:

## 3) R is insoluble

Suppose R is a metal and can thus be considered to be at essentially unit activity ( $a_R=1$ ) as the electrode reaction takes place on bulk R.

### Nernst Equation

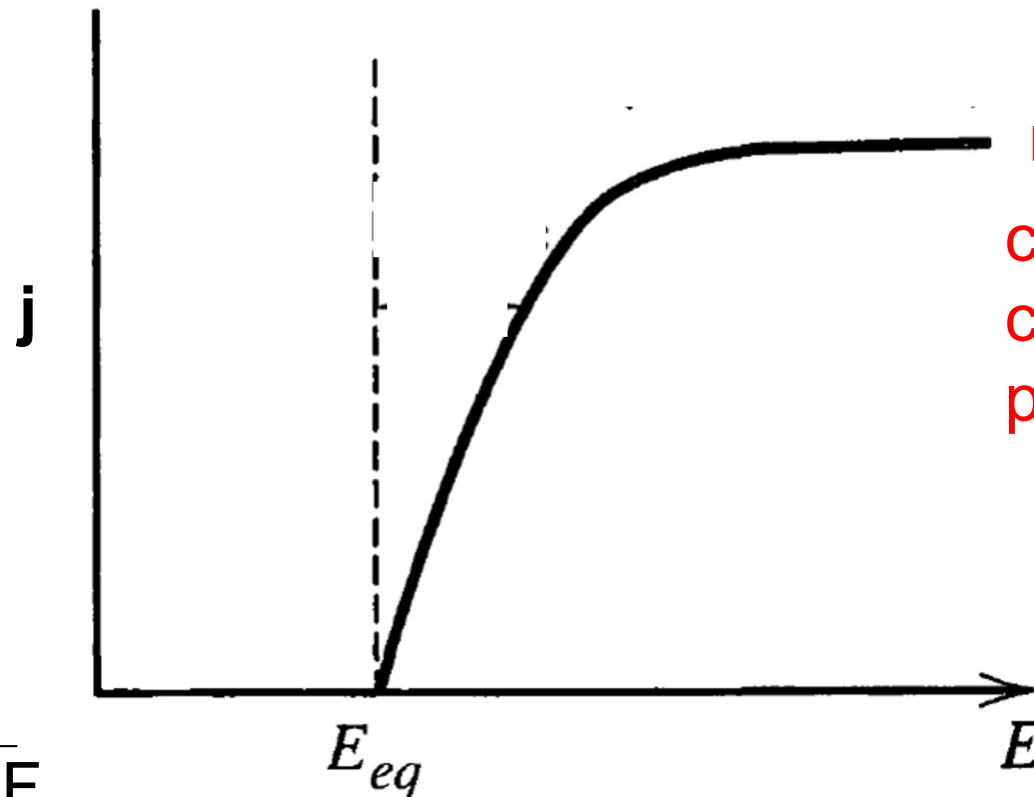
$$E_{\text{cell}} = E^{\circ}_{\text{cell},T} + \frac{RT}{zF} \ln [\text{O}]_s \stackrel{\text{substitution}}{=} E^{\circ}_{\text{cell},T} + \frac{RT}{zF} \ln \left[ [\text{O}^*] \left[ 1 - \frac{j}{j_{\text{lim},c}} \right] \right]$$

$$E_{\text{cell}} = E^{\circ}_{\text{cell},T} + \frac{RT}{zF} \ln [\text{O}^*] + \frac{RT}{zF} \ln \frac{j_{\text{lim},c} - j}{j_{\text{lim},c}}$$

# Linear diffusion approximation: 3) R is insoluble

$$E_{\text{cell}} = E^{\circ}_{\text{cell},T} + \frac{RT}{zF} \ln [O^*] + \frac{RT}{zF} \ln \frac{j_{\text{lim},c} - j}{j_{\text{lim},c}}$$

$\eta_{\text{conc}}$



Recall Chapter 4A  
(slide 28+)

mass transfer resistance

$$R_{\text{mt},c} = \frac{RT}{|j_{\text{lim},c}|zF}$$

# Summary: linear diffusion approximation

**O and R initially present:**

$$E_{\text{cell}} = E^{\circ}_{\text{cell},T} - \frac{RT}{zF} \ln \frac{k_{m,O}}{k_{m,R}} + \frac{RT}{zF} \ln \frac{j - j_{\text{lim},c}}{j_{\text{lim},a} - j}$$

**R initially absent: ( $j_{\text{lim},a} = 0$ )**

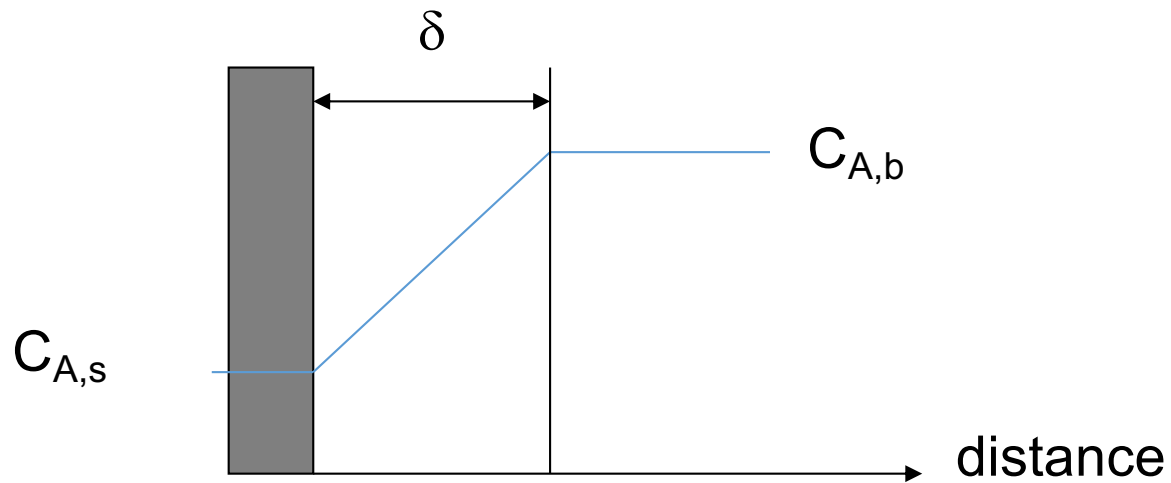
$$E_{\text{cell}} = E^{\circ}_{\text{cell},T} - \frac{RT}{zF} \ln \frac{k_{m,O}}{k_{m,R}} + \frac{RT}{zF} \ln \frac{j - j_{\text{lim},c}}{-j}$$

**O initially absent: ( $j_{\text{lim},c} = 0$ )**

$$E_{\text{cell}} = E^{\circ}_{\text{cell},T} - \frac{RT}{zF} \ln \frac{k_{m,O}}{k_{m,R}} + \frac{RT}{zF} \ln \frac{j}{j_{\text{lim},a} - j}$$

Recall:  $k_{m,O}$ ,  $k_{m,R} \propto \delta(t)^{-1}$ , so they are actually **functions of time**

# Flux $N_A$ of species A normal to the electrode surface



$$N_A = -D_A \frac{C_{A,b} - C_{A,s}}{\delta} \quad (\text{mol/m}^2 \text{ s})$$

$D_A$  : coefficient of diffusion ( $\text{m}^2/\text{s}$ )

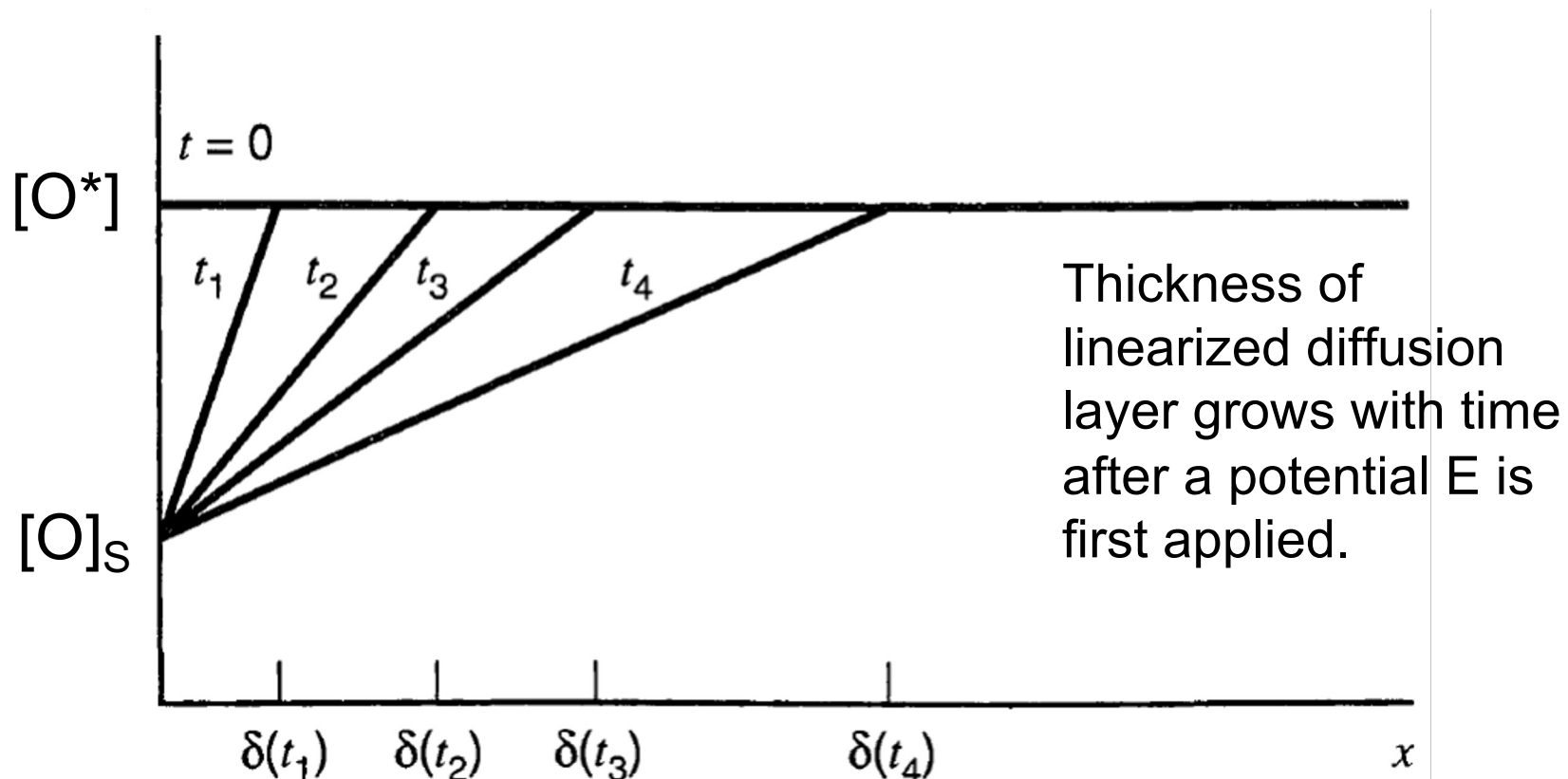
$\delta$  : thickness of Nernst diffusion layer (m)

$$i_{\text{lim}} = \pm z F D_A c_{A,b} / \delta$$

# Linear diffusion approximation: transient response

Now consider the diffusion layer thickness to be a **time-dependent** response:

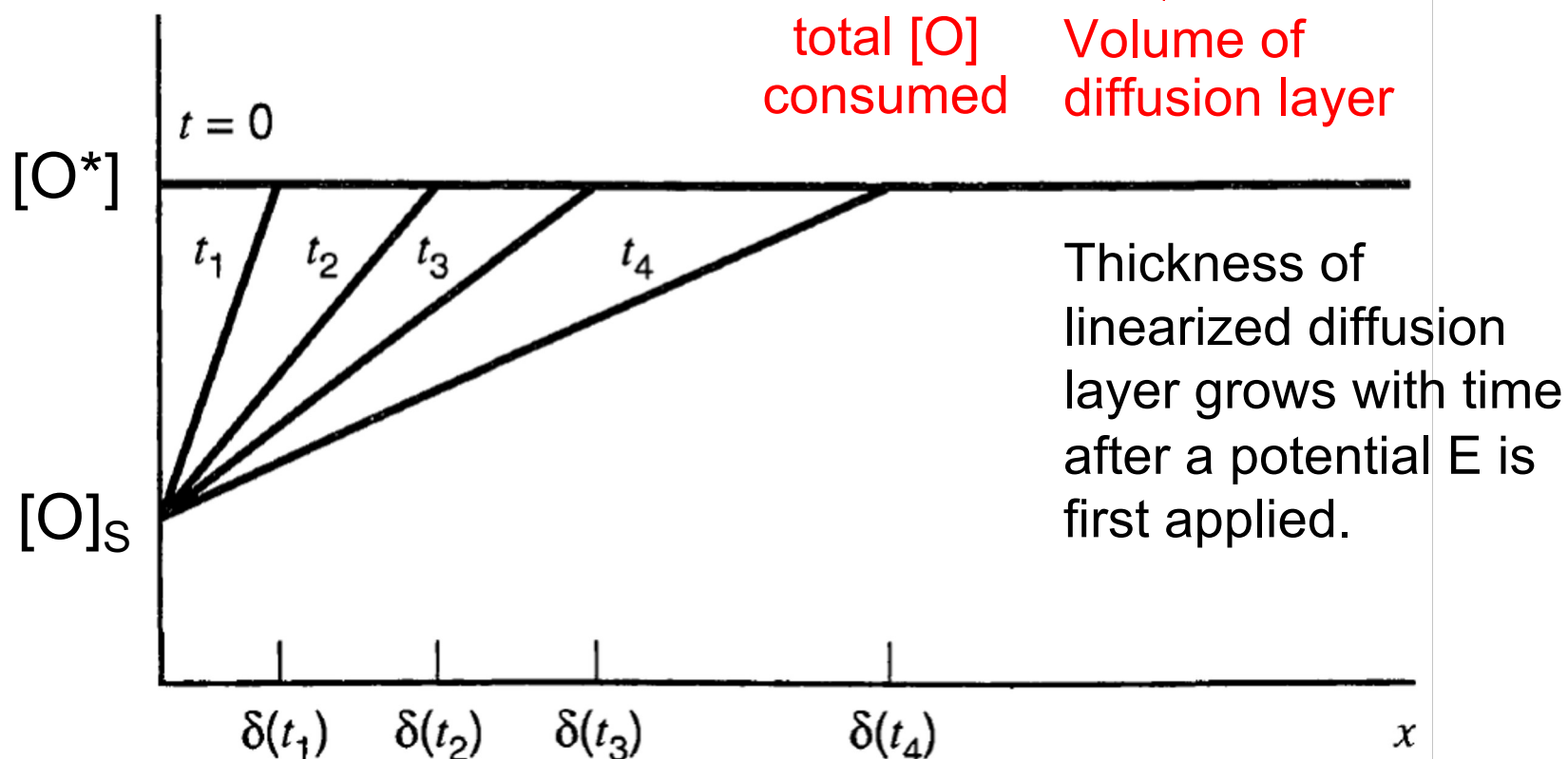
$$\text{mol/m}^2.\text{s} \quad \text{rate of mass transfer (} v_{\text{mt}} \text{)} = \text{rate of reaction (} v_{\text{rxn}} \text{)} = \frac{j}{zF} = \frac{D([O]^* - [O]_s)}{\delta(t)}$$



# Linear diffusion approximation: transient response

The current flow causes a depletion of O, where the amount of O reacted is given by

$$\text{Moles of O reacted in diffusion layer} = \underbrace{([O]^* - [O]_s)}_{\text{total [O] consumed}} \underbrace{\frac{A \cdot \delta(t)}{2}}_{\text{Volume of diffusion layer}} = \int_0^t \frac{i}{zF} dt$$



# Linear diffusion approximation: transient response

The current flow causes a depletion of O, where the amount of O reacted is given by

$$\text{Moles of O reacted in diffusion layer} = ([O]^* - [O]_s) \frac{A \cdot \delta(t)}{2} = \int_0^t \frac{i}{zF} dt$$

$$([O]^* - [O]_s) \frac{A}{2} \frac{d\delta(t)}{dt} = \frac{i}{zF} = \frac{D_O}{\delta(t)} A \cdot ([O]^* - [O]_s)$$

Recall: Chapter 4A  
(linearization of Fick's Law)

$$j = k_{m,O} ([O]^* - [O]_s) \cdot z \cdot F$$

$$\frac{d\delta(t)}{dt} = \frac{2D_O}{\delta(t)}$$

Since  $\delta(t) = 0$  at  $t = 0$ ,

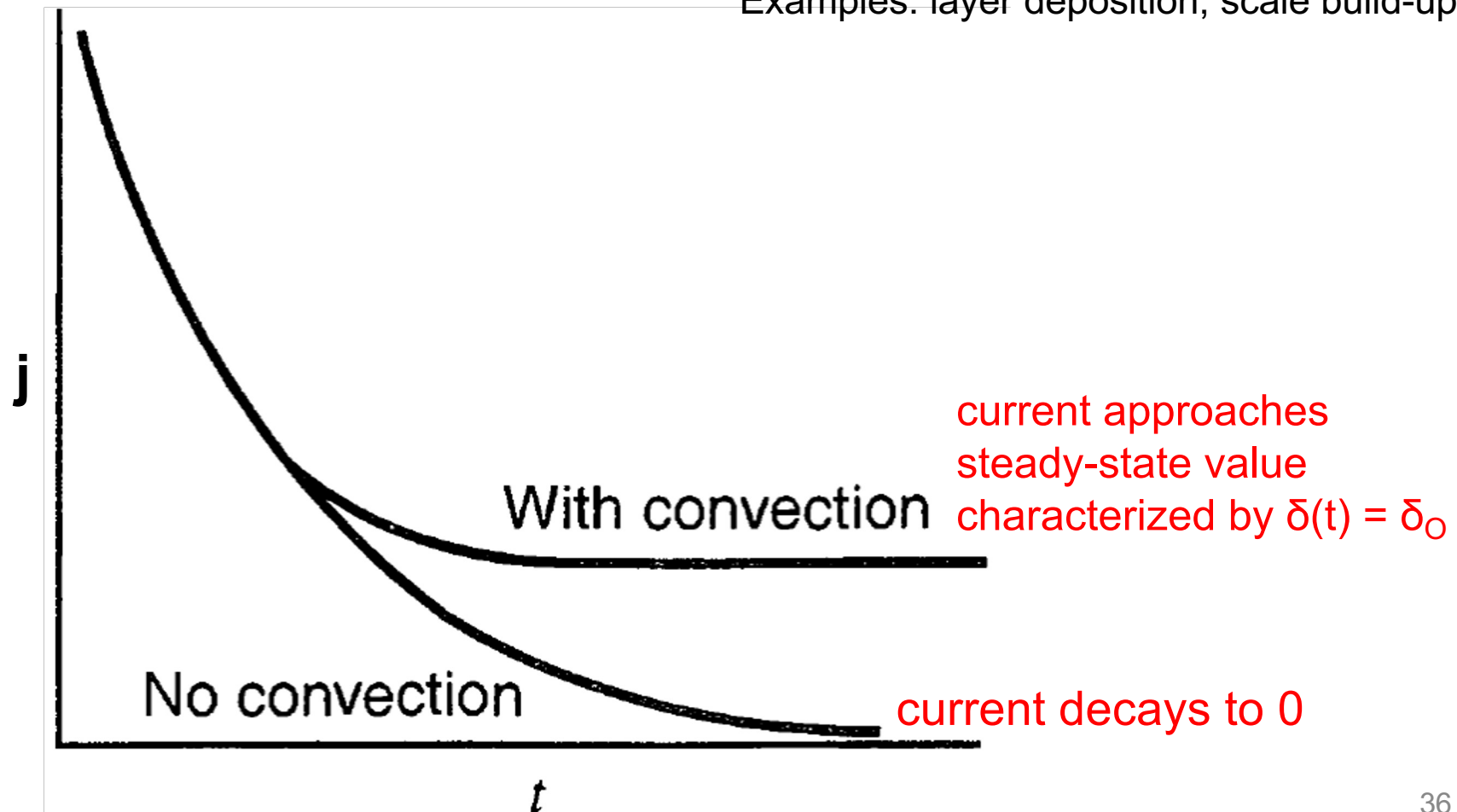
$$\delta(t) = 2(D_O t)^{0.5}$$

$$\frac{j}{zF} = \frac{D_O^{0.5}}{2t^{0.5}} ([O]^* - [O]_s)$$

# Linear diffusion approximation: **transient** response

- $\delta(t)$  increases with  $t^{0.5}$
- $j$  decays with  $t^{-0.5}$

Examples: layer deposition, scale build-up,...



# Diffusion-limited case: rigorous approach

Semi-empirical approach used thus far

## Assumptions

- Nernstian behavior
- $j = k_{m,O}([O]_S - [O^*]) \cdot z \cdot F$
- $j = k_{m,R}([R^*] - [R]_S) \cdot z \cdot F$

Simple  
math



i-E Curve

Can we justify these  
assumptions?

# Diffusion-limited case

## Fick's First Law

$$J_i(x) = - D_i \frac{\partial C_i(x)}{\partial x}$$

## Fick's Second Law

$$\frac{\partial C_i(x,t)}{\partial t} = D_i \frac{\partial^2 C_i(x,t)}{\partial x^2}$$

More generally,

## Fick's First Law

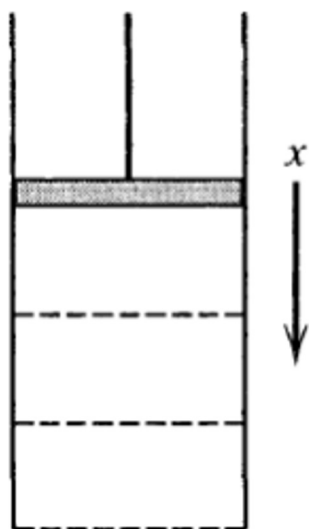
$$J_i = - D_i \nabla C_i$$

## Fick's Second Law

$$\frac{\partial C_i}{\partial t} = D_i \nabla^2 C_i$$

# Linear diffusion-limited case

Consider the first case where we apply a step potential to go from a non-faradaic process to a mass-transport limited process



$$\frac{\partial C_{\text{O}}(x,t)}{\partial t} = D_{\text{O}} \frac{\partial^2 C_{\text{O}}(x,t)}{\partial x^2}$$

1. Initial conditions ( $t = 0$ )  $\longrightarrow C_{\text{O}}(x,0) = [\text{O}^*]$
2. Conditions at far distances ( $x \gg 0$ )  $\longrightarrow \lim_{x \rightarrow \infty} C_{\text{O}}(x,t) = [\text{O}^*]$
3. Conditions at the surface ( $x = 0$ )  $\longrightarrow C_{\text{O}}(0,t) = 0 \quad (t > 0)$

# Diffusion-limited case: rigorous approach

Semi-empirical approach used thus far

## Assumptions

- Nernstian behavior
- Linear profile
- $j = k_{m,O}([O]_S - [O^*]) \cdot z \cdot F$
- $j = k_{m,R}([R^*] - [R]_S) \cdot z \cdot F$

Simple

math

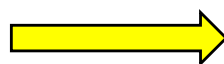


$$\frac{j}{zF} = \frac{D_O^{0.5}}{2t^{0.5}} ([O^*] - [O]_S)$$

## Assumptions

- Nernstian behavior
- Diffusion equations
- Boundary conditions

More  
complex  
math



$$j = \left[ \frac{D_O}{\pi \cdot t} \right]^{0.5} ([O^*] - [O]_S) \cdot z \cdot F$$

# Current density for non-steady state concentration profiles

Case of the cathodic reduction of a species at the electrode:

$$i_c = -n F \left. \frac{d c}{d x} \right|_{x=0}$$

mass transport controlled kinetics, Fick's 1<sup>st</sup> Law  
(current is proportional to the **concentration gradient**)

$$\left. \frac{d c}{d t} \right|_x = D \frac{d^2 c}{d x^2}$$

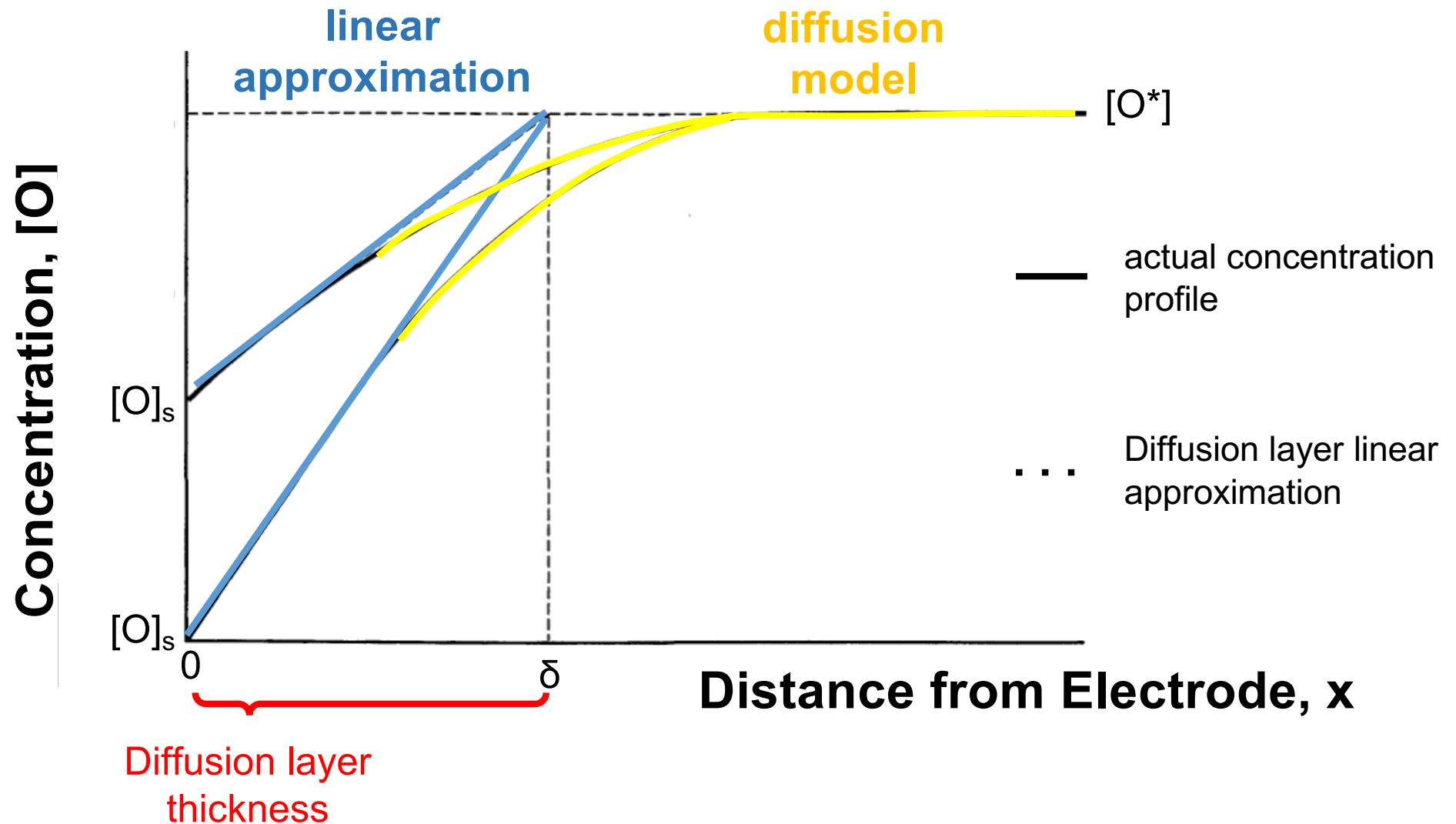
concentration evolution with time, Fick's 2<sup>nd</sup> Law  
(conc. change with t, at position x, changes with the **current gradient** at that position)

Solving the above equation system yields the **Cottrell equation**:

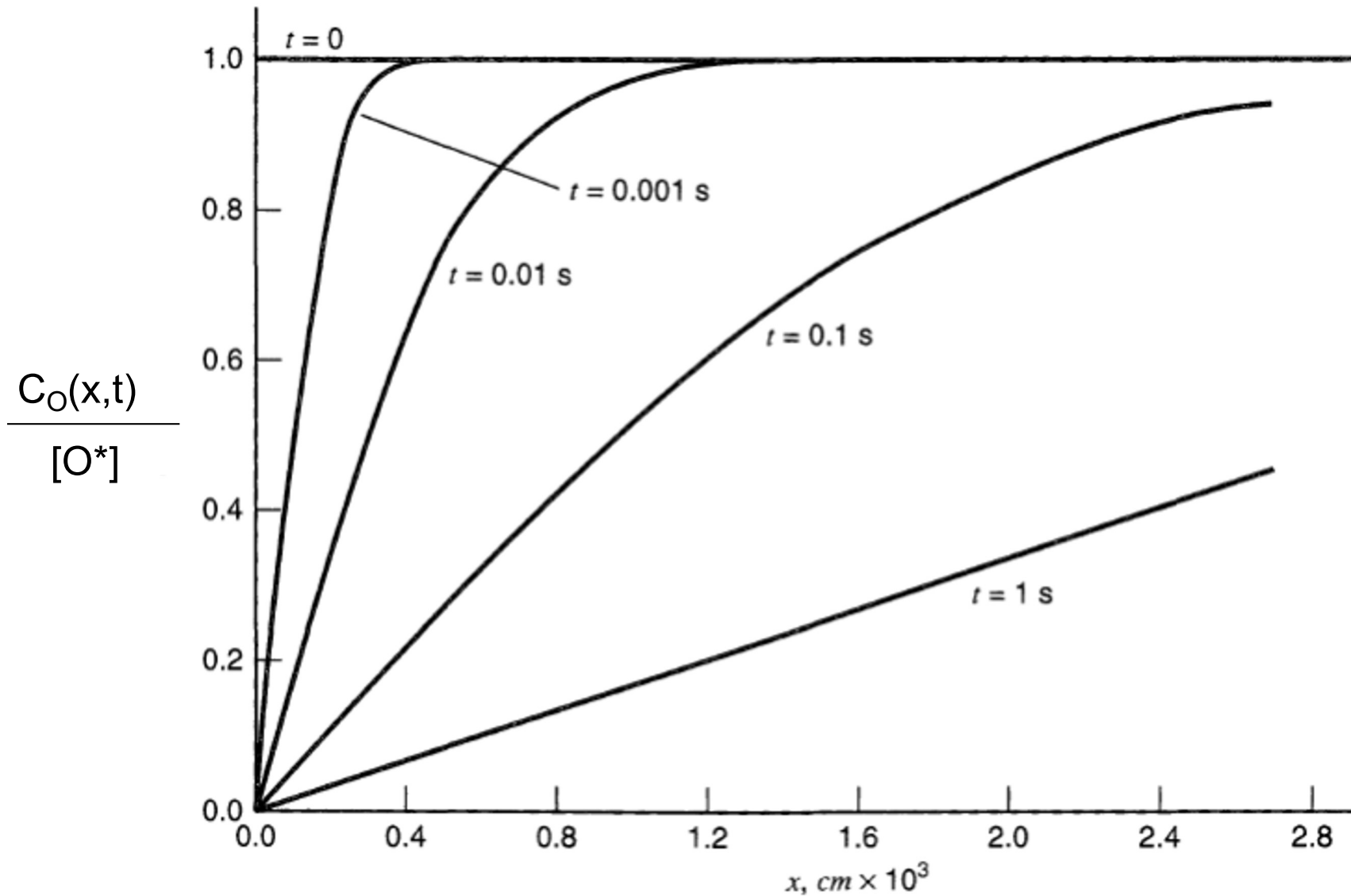
$$i_c = -n F (c_b - c_s) (D/(\pi t))^{0.5}$$

in practice : plot  $i$  vs  $1/\sqrt{t}$ ; (see chapter 5 'Experimental techniques')  
when the result is linear, the reaction is diffusion-controlled,  
and from the slope a diffusion coefficient  $D$  can be extracted

# Diffusion-Limited Case



# Potential Step methods under diffusion control: planar diffusion



# Modes of Mass Transfer

**Diffusion** : Movement of a species under the influence of a gradient of chemical potential (i.e., a concentration gradient).

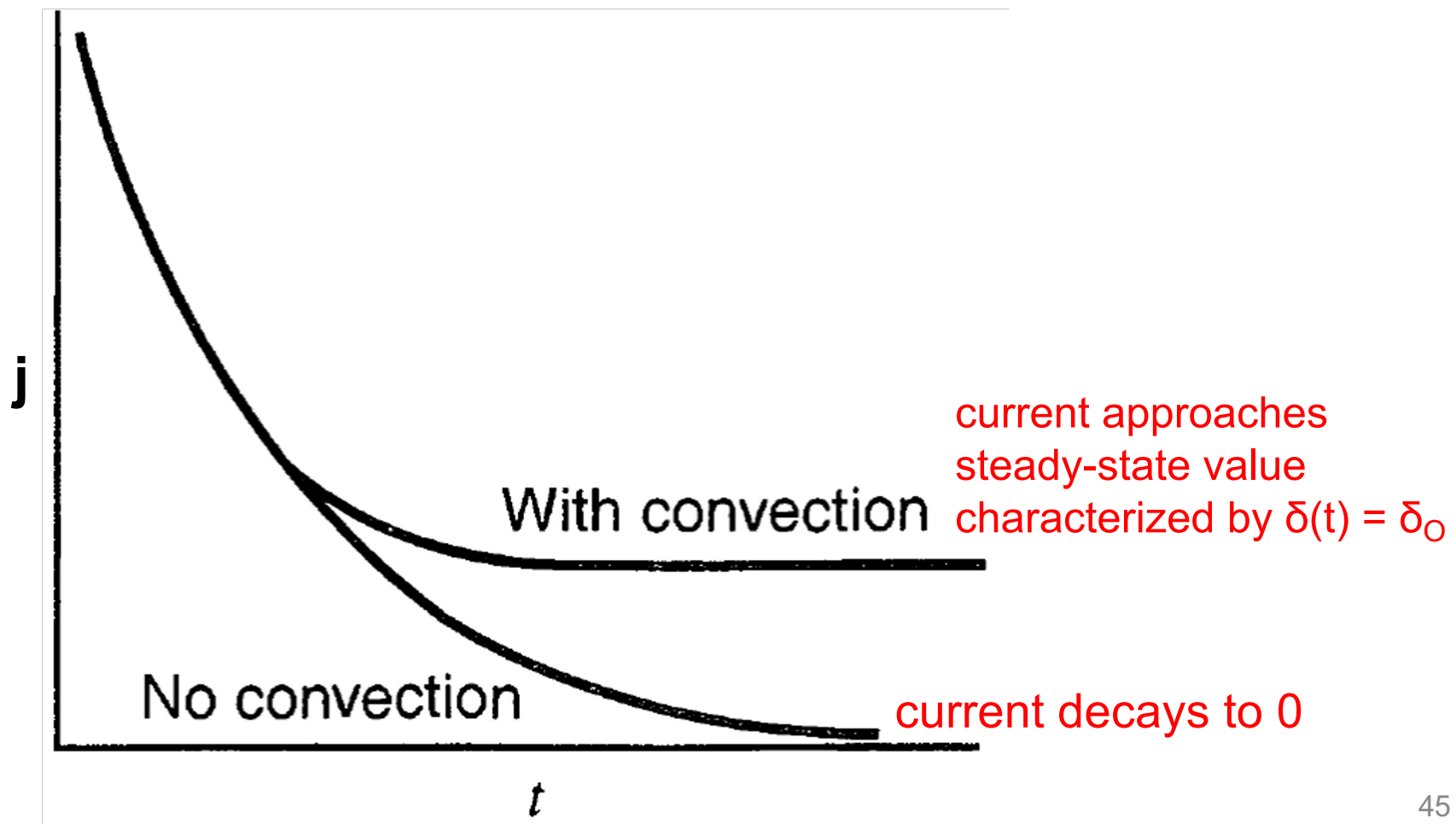
**Migration** : Movement of a charged body under the influence of an electric field (a gradient of electrical potential).

**Convection** : Stirring or hydrodynamic transport (may be characterized by stagnant regions, laminar flow, or turbulent flow).

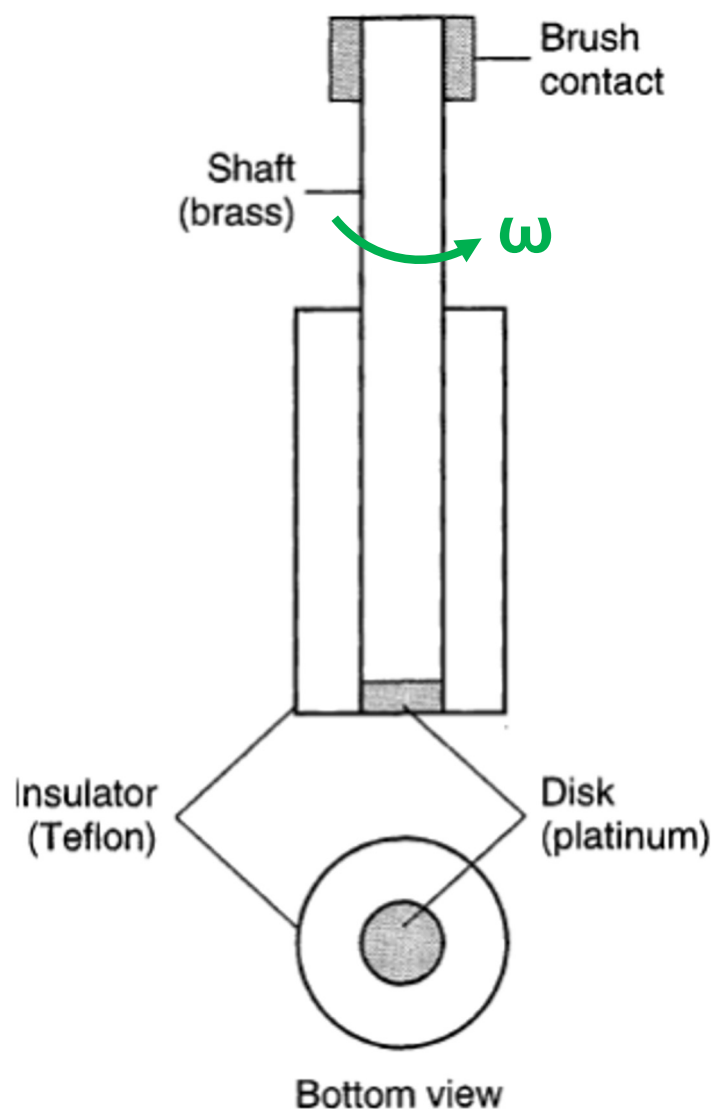
 Rotating disc electrode (RDE)

# Linear diffusion approximation: **transient** response

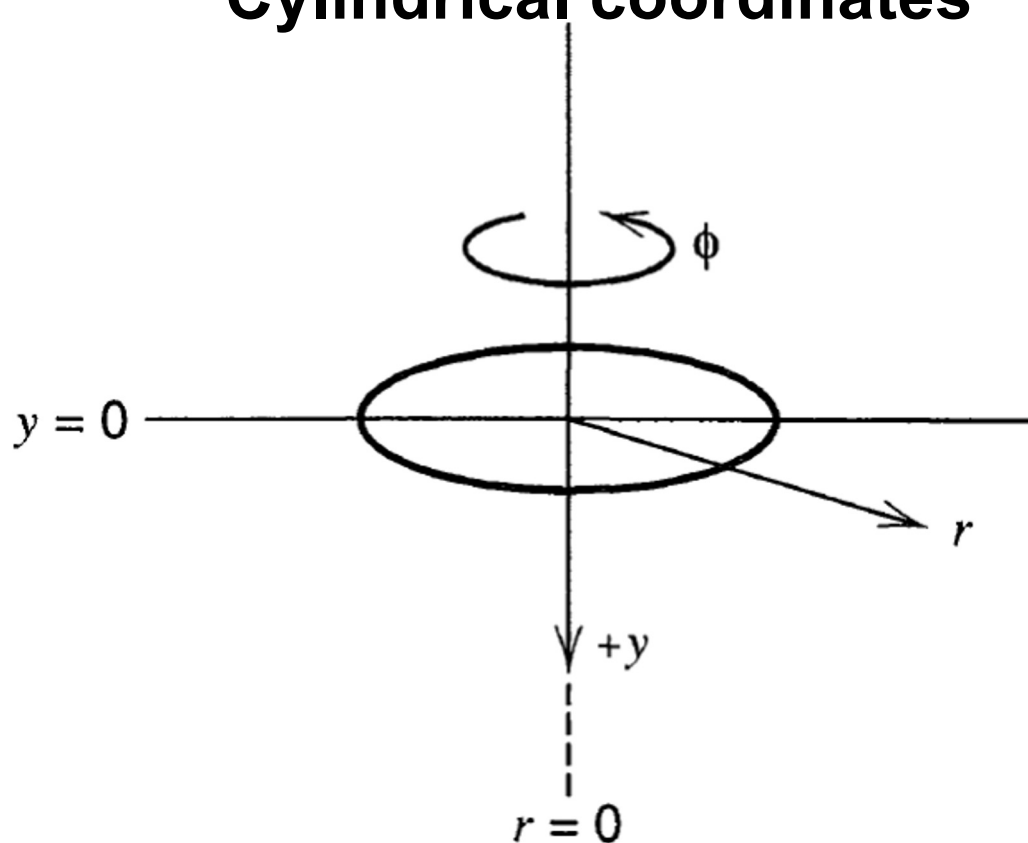
- $\delta(t)$  increases with  $t^{0.5}$
- $j$  decays with  $t^{-0.5}$



# Rotating Disk Electrode (RDE)



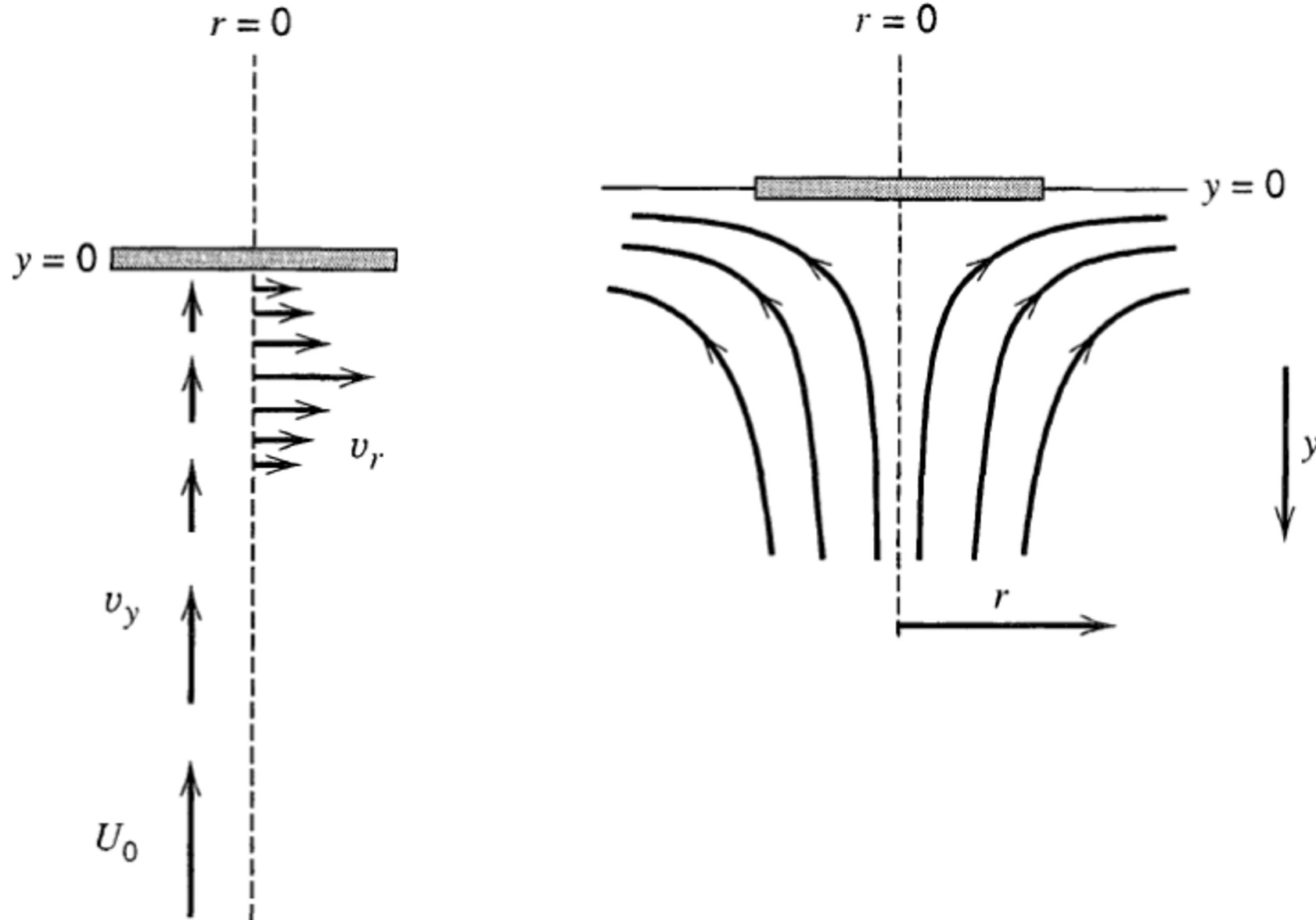
## Cylindrical coordinates



$$\omega = \text{angular velocity (s}^{-1}\text{)}$$
$$= 2\pi N$$

rotation frequency  
[revolutions/s]

# Solving for RDE velocity profile



# Rotating Disk Electrode (RDE)

$$j_{\text{lim},c} = 0.62 z F D_O^{2/3} \omega^{1/2} \nu^{-1/6} [O^*]$$

**Levich Equation**

( $\nu$  = viscosity)

